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Memristive plasticity in artificial electrical synapses *via* geometrically reconfigurable, gramicidin-doped biomembranes†

Subhadeep Koner, ^a Joseph S. Najem, ^b Md Sakib Hasan ^c and Stephen A. Sarles ^{*,a}

It is now known that mammalian brains leverage plasticity of both chemical and electrical synapses (ES) for collocating memory and processing. Unlike chemical synapses, ES join neurons *via* gap junction ion channels that permit fast, threshold-independent, and bidirectional ion transport. Like chemical synapses, ES exhibit activity-dependent plasticity, which modulates the ionic conductance between neurons and, thereby, enables adaptive synchronization of action potentials. Many types of adaptive computing devices that display discrete, threshold-dependent changes in conductance have been developed, yet far less effort has been devoted to emulating the continuously variable conductance and activity-dependent plasticity of ES. Here, we describe an artificial electrical synapse (AES) that exhibits voltage-dependent, analog changes in ionic conductance at biologically relevant voltages. AES plasticity is achieved at the nanoscale by linking dynamical geometrical changes of a host lipid bilayer to ion transport *via* gramicidin transmembrane ion channels. As a result, the AES uniquely mimics the composition, biophysical properties, bidirectional and threshold-independent ion transport, and plasticity of ES. Through experiments and modeling, we classify our AES as a volatile memristor, where the voltage-controlled conductance is governed by reversible changes in membrane geometry and gramicidin channel density. Simulations show that AES plasticity can adaptively synchronize Hodgkin–Huxley neurons. Finally, by modulating the molecular constituents of the AES, we show that the amplitude, direction, and speed of conductance changes can be tuned. This work motivates the development and integration of ES-inspired computing devices for achieving more capable neuromorphic hardware.

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Introduction

Two-terminal synaptic devices hold promise to store and process information at significantly lower energy cost than three-terminal devices.^{1–4} By emulating threshold-dependent conductance changes and multi-timescale memory and plasticity found in their biological counterparts, artificial synapses could radically transform computing hardware by mimicking the way the brain learns, remembers, and processes information through activity-dependent plasticity⁵—originally

believed to be present only in chemical synapses. Accordingly, research to develop synapse-inspired computing devices has produced material systems, including non-volatile memristors^{6–8} with hysteretic current–voltage relationships, that inherently mimic the discrete, threshold-dependent conductance switching used by chemical synapses.

In contrast, electrical synapses (ES) have long been thought to form fixed-conductance connections (modeled as resistors) between neurons. However, it was recently reported that the magnitude of electrical coupling (*i.e.*, proportional to synapse conductance) between neurons connected *via* electrical synapses can vary significantly through activity-dependent plasticity^{9–11} to control the level of synchronization in neural networks. Similar to their chemical counterparts, ES exhibit multiple forms of plasticity (*e.g.*, facilitation, depression) at timescales ranging from milliseconds to days.¹² For example, coupling between retinal photoreceptors can be very low in complete darkness or bright light and significantly elevated at moderate light intensities.^{13,14} This variation enhances the sensitivity of

^aDepartment of Mechanical, Aerospace and Biomedical Engineering, University of Tennessee, Knoxville, Tennessee 37916, USA. E-mail: ssarles@utk.edu; Tel: +1 865-974-3488

^bDepartment of Mechanical Engineering, The Pennsylvania State University, University Park, Pennsylvania 16802, USA

^cDepartment of Electrical Engineering, University of Mississippi, Oxford, Mississippi 38677, USA

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retinal circuits during transitioning between nighttime and daytime visual tasks.

ES are composed of gap junctions, aligned protein hemichannels (*e.g.*, connexins or innexins) contributed from adjacent cells,^{15,16} that span the 2–4 nm gap between plasma membranes. These water-filled structures mechanically and electrically link neurons^{17,18} as illustrated in Fig. 1A. Unlike the voltage-triggered release of neurotransmitters in chemical synapses, the pre-synaptic terminal of an electrical synapse does not have to cross a firing threshold to transmit an action potential.¹⁹ Instead, ions diffuse passively through the always-open hemichannels to cells at lower potentials. The lack of a threshold enables quicker communication and sharing of action potentials. While always conductive, the conductance (*i.e.*, coupling) of an electrical synapse is not static, but rather continuously variable. The coupling level between neurons is often measured as the ratio of voltages accumulated in both

the pre- and post-synaptic neurons.²⁰ These dynamic variations in coupling levels instill modulation of both the temporal and spatial transmission of information exchange.²¹ Mechanistically, electrical synapse plasticity can result from dynamic alterations of existing connexin conductance states,^{22–24} increases or decreases in number of connexin channels,^{25–27} and modification of passive and active membrane properties by synaptic inputs.^{28–31}

Undoubtedly, the superior cognitive ability of the brain stems from collective functionalities of networks of chemical and electrical synapses adapting and communicating together. However, brain-inspired materials and neuromorphic devices seeking to achieve signal processing, learning, and memory capabilities of the brain have predominately focused on two- or three-terminal devices (*e.g.*, memristors, transistors) with voltage-controlled, threshold-dependent changes in electrical/ionic conductance.² The vast majority of these systems exhibit

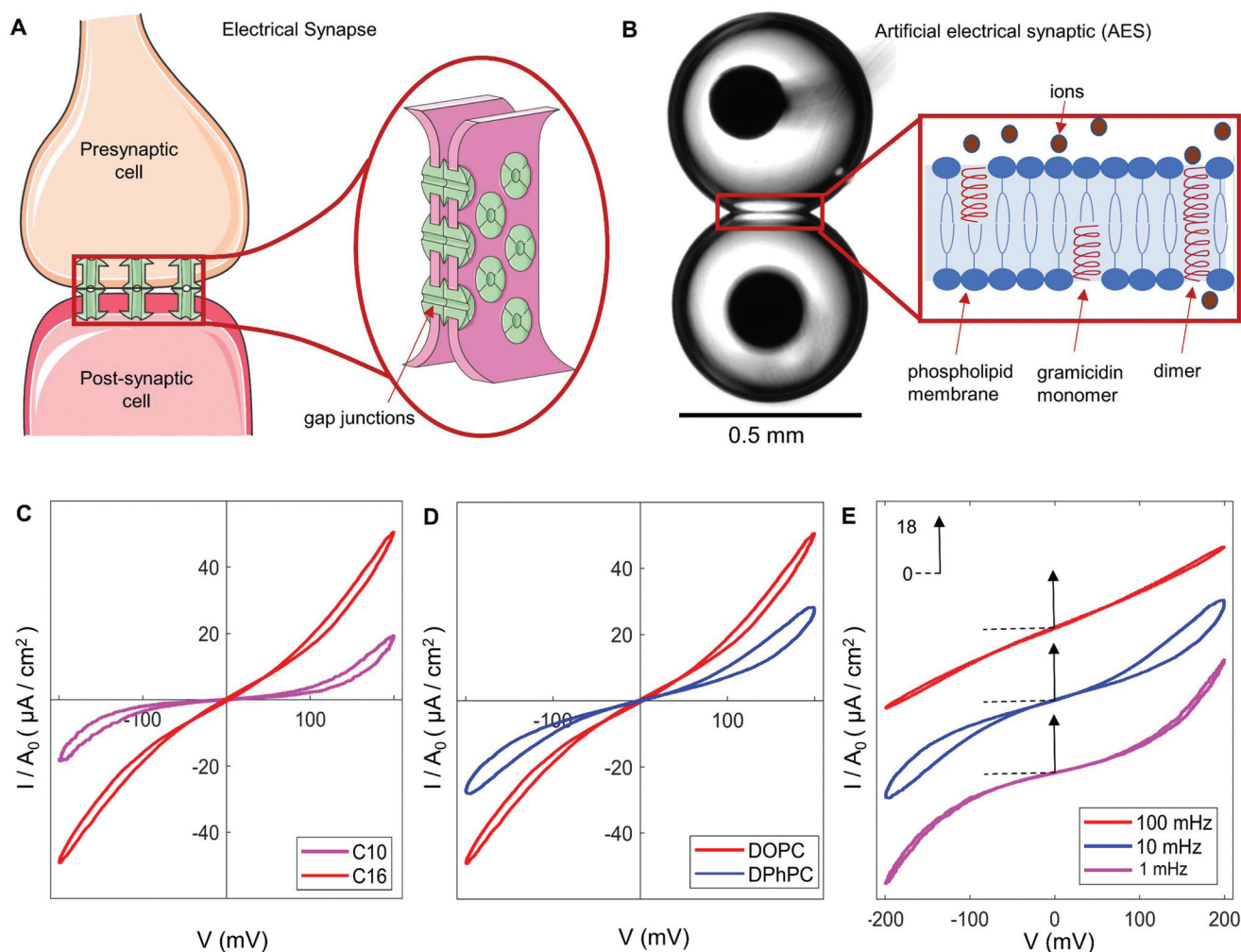


Fig. 1 Two-terminal AES exhibiting nonlinear memristive behavior. (A) Cartoon depicting ES gap junctions formed by connexin hemichannels. (B) Biomolecular AES with gramicidin monomers dimerizing end-to-end to form channels for ion passage (inset) through the membrane. I – V relationships for: (C) DOPC AES assembled in two different oils: hexadecane (red) and decane (magenta); (D) AES formed in hexadecane from either DOPC or DPhPC lipids; and (E) DPhPC AES in hexadecane. All currents are normalized per zero-volt initial area, A_0 . Applied bias consisted of a 200 mV bipolar sinusoidal voltage at 10 mHz, unless stated otherwise.

sharp threshold-dependent switching^{32,33} between a small number of discrete conductance states,^{6,33–38} thereby implicitly mimicking the functionalities of chemical synapses.^{39,40} On the other hand, the development of threshold-independent synaptic devices with activity-controlled, analog changes in conductance has received far less attention.⁴¹

Here, we present an artificial electrical synapse (AES) constructed with a 5 nm-thick synthetic bio-membrane containing voltage-independent, pore-forming gramicidin peptides. Like biological ES, this assembly permits bidirectional ion transport *via* always-open channels and exhibits voltage-dependent memory resistance, with continuous conductance variations that occur across nominal ranges of 22–160 pS¹⁶ and at biologically-relevant voltages. This contribution builds on our recent work,⁴² which demonstrated that insulating, lipid-only biomembranes formed between lipid-coated aqueous droplets in oil exhibit hysteretic, geometric reconfigurations stemming from voltage-driven modulation of membrane area and thickness. Introducing gramicidin peptides into the membrane creates always-conductive transmembrane ion channels similar to gap junctions—transforming the capacitive membrane into a memristive one that exhibits a pinched, hysteretic current–voltage relationship and displays short-term plasticity to successive voltage pulses. Experiments and modeling are performed to assess changes in membrane geometry and gramicidin channel densities in response to voltage and to explain the sources of resistance hysteresis and short-term plasticity. These allow us to show that the dynamic geometrical reconfigurations of the membrane dictate the rates of current–voltage hysteresis, even though the density of gramicidin channels also increases with applied voltage. Finally, we demonstrate through both experiments and modeling that the AES can be modularly configured to exhibit paired-pulse depression and that voltage-induced plasticity in conductance can synchronize the firing of Hodgkin–Huxley neurons.

Results and discussion

A gramicidin-doped lipid membrane has similar structure and composition to biological ES

Inspired by the biomolecular memristor featuring voltage-activated alamethicin channels⁴³ and the capacitive, lipid-only biomolecular memcapacitor,⁴² the artificial electrical synapse (AES) studied herein represents a modular variation of those prior embodiments, one that is also based on a planar lipid bilayer membrane formed at the interface between two lipid-coated aqueous volumes in oil (also known as a droplet interface bilayer (DIB), see Experimental). Specifically, the ~5 nm-thick, insulating membrane is doped with gramicidin peptides that spontaneously insert^{44,45} in the absence of voltage into the membrane where monomers in each leaflet align end-to-end to form water-filled, conductive channels across the membrane. Illustrated in Fig. 1B, this end-to-end alignment and the resulting ionic conductivity achieved with gramicidin channels closely mimic the structural configuration and voltage-

independent transport properties of connexins in ES. Also, like gap-junctions in ES, this AES is always in a conductive (active) state.

Current–voltage relationships reveal memristive behavior

The hypothesis motivating this study is that the voltage-dependent geometric reconfigurations we observe in lipid-only membranes provides a lever for affecting the number of gramicidin channels in the membrane to instill activity-dependent plasticity like in ES. Therefore, to characterize these responses and reveal the effects of lipid and oil types, we measure the current, I , induced by a sinusoidal voltage, V , on gramicidin-doped membranes constructed separately from two types of synthetic lipids (diphytanoyl phosphatidylcholine, DPhPC, and dioleoyl phosphatidylcholine, DOPC) that form stable lipid bilayers⁴⁶ and two different alkane oils (hexadecane, C16, and decane, C10) that result in varying sensitivities to voltage-driven changes in membrane area and thickness.⁴² Representative I – V responses for final gramicidin concentrations of 0.5 μM in each droplet are shown in Fig. 1C–E, with the current normalized by the zero-volt membrane area to minimize effects of differing starting synapse areas.

For all combinations, we measure pinched, hysteretic I – V loops at frequencies less than 50 mHz. Fig. 1C shows that DOPC AES in C10 exhibit stronger nonlinearity and larger hysteresis when compared to C16. Moreover, the instantaneous slopes of these data show that the DOPC AES in C10 exhibits relatively higher ohmic resistance (86 $\text{k}\Omega \text{ cm}^2$) near 0 V (flatter) and lower resistance (12 $\text{k}\Omega \text{ cm}^2$) near |200 mV| (steeper). In C16, both DOPC AES and DPhPC AES exhibit less variation in resistance *versus* voltage: 10 $\text{k}\Omega \text{ cm}^2$ and 17 $\text{k}\Omega \text{ cm}^2$ near 0 V, respectively, to 6.6 $\text{k}\Omega \text{ cm}^2$ and 9 $\text{k}\Omega \text{ cm}^2$ near 200 mV, respectively. In comparison, lipid-only membranes lacking gramicidin exhibit significantly higher resistances of 10–100 $\text{M}\Omega \text{ cm}^2$ and do not exhibit I – V hysteresis at frequencies below 50 mHz (see Fig. S2†). Since the conductance of a gramicidin channel is relatively constant (5.8 pS),^{47,48} this suggests the number of gramicidin channels per unit area in DOPC AES in C10 is less than in a DOPC AES in C16.

Fig. 1D compares the responses of AES formed from the two different lipids types (DPhPC and DOPC) in C16. Here, we see that a DOPC AES displays less I – V hysteresis and higher conductance, signifying a higher gramicidin channel density than in DPhPC. This difference is consistent with and can be explained by prior research which demonstrated that gramicidin channels have higher affinity⁴⁹ for and greater stability (*i.e.*, channel lifetime)⁵⁰ in DOPC membranes compared to DPhPC bilayers.

These measurements also reveal the frequency of the applied voltage sweep affects the shape and hysteresis of the I – V relationship. The representative data in Fig. 1E for a DPhPC AES in C16 show that the I – V response is most non-linear at the lowest frequency (1 mHz) and the most linear at 100 mHz. These data also show that hysteresis is minimal at both the lowest and highest frequencies tested and significantly greater at the middle frequency of 10 mHz. While not

shown, the same trend is observed for membrane-based AES constructed with DOPC or using C10. The disappearance of hysteresis at very low frequencies demonstrates that resistive hysteresis in the AES is volatile.

Moreover, unlike our prior study⁴³ using alamethicin-doped membranes that exhibited strong voltage-dependent increases in conductance and high nominal OFF resistances ($>1\text{ G}\Omega$, when channels fully exited the membrane), these data show that gramicidin membranes are always conductive ($\leq 86\text{ k}\Omega$), even at low voltages—just like ES. These trends remain across gramicidin concentrations (see Fig. S3†), which merely scales the number of channels in the interface, proportionally increasing the conductance of the membrane.

Chua established that the fingerprint of a memristor is a pinched hysteresis loop on an I - V plane at certain frequencies and initial conditions when subjected to a voltage or current signal producing a periodic response of similar frequency.^{3,51–53} Therefore, the results in Fig. 1 prove that a gramicidin-doped AES is a volatile memristor, one in which the I - V shape, hysteresis, and frequency range of memristance can be tuned based on membrane composition and also the oil surrounding the droplets. In the context to synaptic plasticity, the hysteresis implies that the conductance of the membrane depends on its prior history of excitation, not just the present stimulus. And unlike the pinched, hysteretic I - V responses measured previously using alamethicin-doped membranes that exhibited exponential increases in current only at voltages above an insertion threshold for the peptides, these AES do not require a specific threshold to become conductive. The modulations in AES resistance are also continuously variable, unlike most solid-state memristors that demonstrate discrete switching.⁵⁴

Modelling gramicidin-doped membrane AES

As depicted in Fig. 1C–E, gramicidin-doped membranes exhibit pinched and hysteretic current induced by a symmetric sinusoidal bias. Since the passage of ions is mediated by gramicidin dimers in the bilayer, these measurements indicate that nominal conductance of the membrane and thus the total number of dimers present depends on both voltage and time.

We know that the membrane elastically reconfigures in response to a nonzero membrane voltage.^{42,55} These reversible changes occur with time constants on the order of seconds and can result from formation of new membrane area due to electrowetting (EW) and a reduction in hydrophobic thickness caused by electrocompression (EC). While not explicitly linked, these geometrically changes are implicitly coupled by the fact that changes in membrane thickness modifies the effective forces driving both EW and EC.⁴² The fact that our data show larger currents upon a decrease in voltage from a maximum value compared to an increase from zero is consistent with the idea that a recent increase in membrane area driven by EW and a decrease in membrane thickness from EC could help to increase the total number of gramicidin dimers present in the interface. Another possibility is that the kinetics of gramicidin insertion, and thus the net number of channels present at

equilibrium, are themselves functions of voltage (or membrane thickness) as is common in many other types of ion channels.

To properly identify and separate these mechanisms driving voltage-induced plasticity, we perform a series of experiments to quantify changes in membrane geometry (area and thickness) and area-normalized channel density as a function of voltage. The dynamics and sensitivities of these variables are assessed by applying stepwise voltages. Membrane area is tracked *via* bottom view images of the AES, and membrane capacitance is determined from the amplitude of ac current induced by a superimposed ac voltage.^{42,56}

Fig. 2A shows a representative measurement of dynamic membrane area normalized to its zero-volt initial value, A_0 , for a 200 mV, 10 mHz sinusoidal bias. The hysteresis observed here suggests that voltage-driven variations in channel density are not alone in causing the observed I - V hysteresis. Similar to the responses in Fig. 1E, dynamical variations and hysteresis become very small at frequencies higher than 100 mHz (Fig. 2A). And while hysteresis disappears at frequencies below 1 mHz (not shown), nonlinear quasi-static changes with respect to voltage become maximal at low frequencies.⁴²

Stepwise changes (0 to +200 mV) in voltage yield exponential rises in area (Fig. S4†), which we used to determine the characteristic time constant for EW, τ_{ew} , for the two lipids and oils (Table 1). These results indicate that EW-induced growth in membrane area is faster for DOPC lipids compared to DPhPC, and for C10 compared with C16. The former is likely the result of greater lipid acyl chain flexibility and mobility that enables faster oil exclusion and rearrangement upon bilayer formation,⁵⁷ while the latter is the result of lower viscosity in C10.⁴² At equilibrium, bilayer area increases linearly with respect to the square of voltage (*i.e.* polarity does not matter),^{55,56,58} where the slope, α , denotes the EW coefficient. The data in Fig. 2B and the average α values in Table 1 show that DOPC membranes in both C10 and C16 exhibit larger fractional changes in area with voltage compared to DPhPC membranes. Further, DOPC membranes formed with droplets in C10 exhibit a slightly higher area change than those formed with droplets submerged in C16. These differences are likely the result of DOPC membranes having higher monolayer and bilayer tensions and, thus, smaller zero-volt areas, which we show in Fig. S5† results in larger fractional increases in bilayer area with voltage.

We also assess changes in the hydrophobic thickness of these membrane AES by measuring the specific capacitance of the membrane *versus* bias using a method described elsewhere.^{56,59} Fig. 2C shows that gramicidin-doped DPhPC membranes in C16 exhibit relatively constant membrane thickness *versus* voltage up to $|\pm 160\text{ mV}|$, whereas gramicidin-decorated DOPC membranes in both C16 and C10 become significantly thinner (15% and 30%, respectively) at higher biases. In the absence of gramicidin, DOPC membranes are also relatively thicker at zero volts, which is attributed to greater oil retention in the hydrophobic region of the membrane upon bilayer formation compared with DPhPC as shown for lipid-only membranes in Fig. S6.† The larger initial thickness and

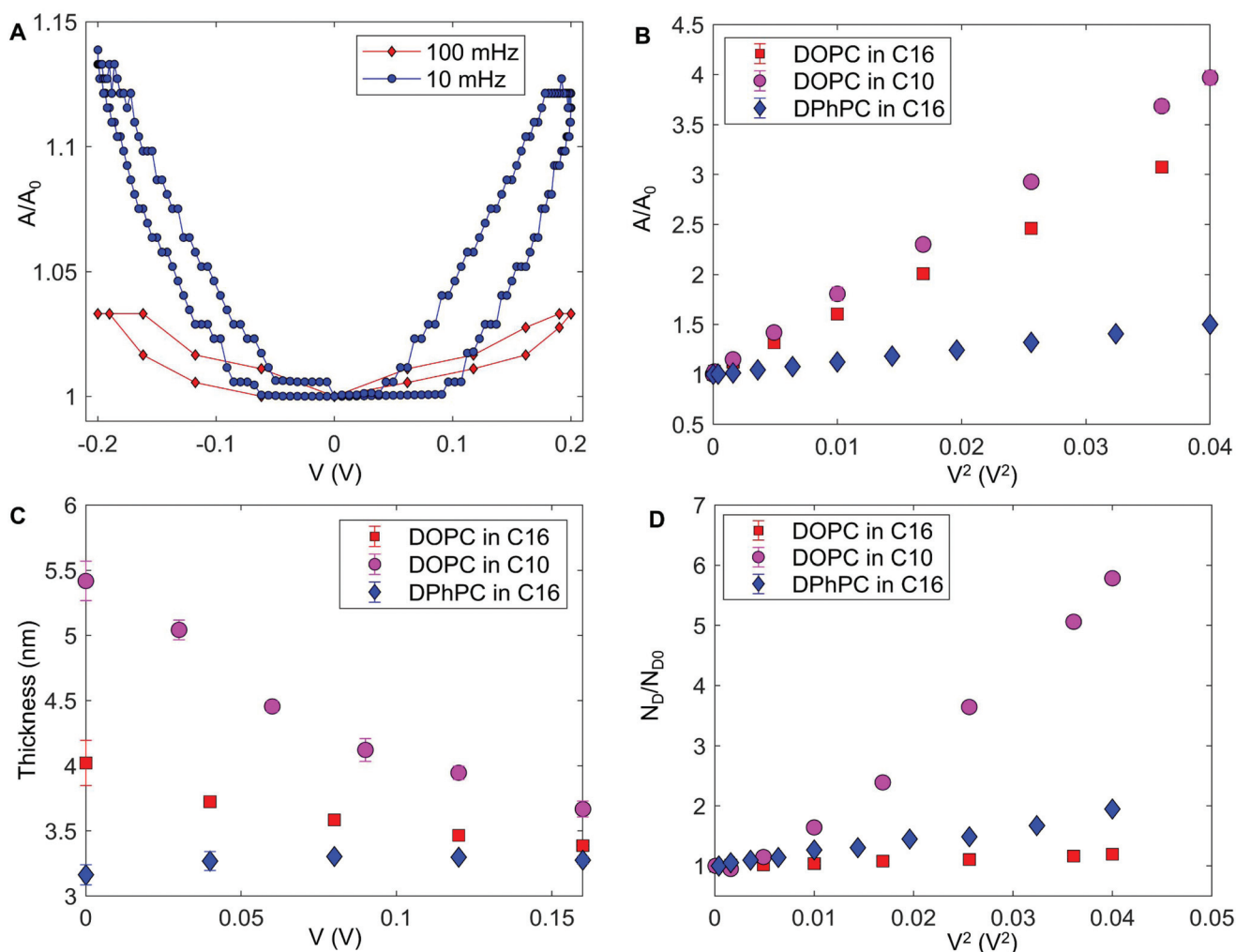


Fig. 2 Characterization of the state variables at steady-state EW and EC conditions. (A) Hysteretic geometric reconfiguration of the membrane interface when stimulated with a sinusoidal input bias voltage of 200 mV at different sweep rates, evaluated as mean of three (steady-state EW) cycles. (B) Response of the normalized area over initial area (at 0 mV) to step increase of bias voltage. (C) Relative thinning of the membrane due to EC for different lipids in different oils in response to step increase in bias voltages. (D) Relative channel density (normalized over 0 mV conditions) at the membrane interface for different lipid types in different oil environments.

Table 1 Summary of EW, EC, and gramicidin channel density dependencies on voltage

Membrane/oil	EW area growth		EC thinning τ_{ec} (s)	Channel density ($\times 10^6$)
	τ_{ew} (s)	$\alpha(V^{-2})$		
DPhPC/C16	14.0 ± 0.3 ($n = 5$)	12.4 ± 0.5 ($n = 4$)	N/A	$N_d(V) = 220V^2 + 10$
DOPC/C16	5.9 ± 0.3 ($n = 5$)	56.5 ± 0.5 ($n = 4$)	40 ± 0.7 ($n = 3$)	$N_d(V) = 220V^2 + 17$
DOPC/C10	1.8 ± 0.2 ($n = 3$)	75.3 ± 0.2 ($n = 4$)	22.3 ± 0.5 ($n = 3$)	$N_d(V) = 300V^2 + 2$

steeper reduction in thickness with voltage for C10 is due to the fact that smaller molecule oils are retained in larger fractions in lipid bilayers.^{42,60} These trends, along with the fact that no significant change in thickness is recorded for DPhPC membranes containing <10% C16 by volume,^{42,56} suggest that EC alters the thickness by compressive oil exclusion, not distortion or compression of the lipid molecules themselves.⁴² While not shown, we have previously demonstrated that this

mechanism for thickness reduction occurs on time scales of 5–25 s, slower than changes in area by EW.⁴²

The conducting unit in our system consists of a dimer (D) formed by two gramicidin monomers (M), aligned end-to-end across the thickness of the membrane.^{61–63} Dimerization can be written as a reversible reaction given by,



with separate forward and reverse reaction rate constants, k_R and k_D , respectively, that depend on membrane composition, temperature, ion concentration, *etc.*⁴⁴ The accumulation of dimers (per unit area) in the system is thus given by:

$$\frac{dN_D}{dt} = k_R N_M^2 - k_D N_D. \quad (2)$$

Assuming the total concentration (mol cm⁻²) of gramicidin in the interface is conserved ($N = N_M + 2N_D$), the population of gramicidin in each leaflet of the bilayer reaches an equilibrium of non-conducting (M) and conducting (D) units at fixed conditions.

Gramicidin channel formation does not require voltage, however prior research has established that k_R and k_D do vary with voltage. As a result, changing the voltage causes a transient reorganization of M and D to establish a new equilibrium in the system, where the time constant of this transient depends on the nominal values of k_R and k_D . Specifically, the fraction of conductive channels in a membrane increases with decreasing membrane thickness⁶⁴—signifying that k_R increases with voltage.⁴⁴ Because k_D also decreases with increasing voltage,⁴⁴ the speed of dimer formation (dN_D/dt) also increases at higher applied biases and at high peptide concentrations. With C16 (*i.e.*, constant thickness), and at the relatively high peptide concentrations used in our study, channels insert in the absence of voltage and reach equilibrium at all fixed voltage levels in less than 5 ms (Fig. S7†). This is considerably faster than the kinetics observed by Bamberg and Lauser, in which a peptide concentration of only 2 nM was used.⁴⁴

These trends, along with the thinning responses in Fig. 2C, are consistent with the likelihood that an increase of the applied voltage in our system favors a higher density of channels in the membrane, and thus higher conductivity. To confirm and quantify this relationship, we measure the nominal current at equilibrium through our gramicidin doped membranes at multiple potentials. Dividing the current by the product of the applied potential, V , the unit conductance of one dimer, G_u , and the equilibrium area of the membrane at each voltage allows us to compute the channel density per unit area *versus* voltage (see Fig. 2D and Fig. S8†). Here, we see that channel density increases linearly with respect to voltage squared and that a DOPC membrane in C10 exhibits a larger fractional increase in channel density compared to either DOPC or DPhPC bilayers in C16. This finding is consistent with the fact that DOPC membranes in C10 retain more oil and, thus, exhibit greater fractional decreases in thickness with increasing voltage. The nominal data in Fig. S8† also highlight the higher number of dimers in DOPC bilayers *versus* DPhPC and the higher number of channels in DOPC for C16 *versus* C10. The former is consistent with prior work^{49,50} which demonstrated a higher affinity of gramicidin with unsaturated DOPC lipids compared to DPhPC lipids, while the latter agrees with results by Hladky and Haydon which demonstrated that thinner membranes yield higher association rate constants and more dimers at equilibrium.⁴⁷

Based on these data, it is clear that both voltage-driven growth (fractional) in membrane area, A_m , and channel density, N_D , are the two states that influence the total nominal conductance, G , of the membrane as given by:

$$I = G(N_D, A_m)V. \quad (3)$$

Without a direct relationship between thickness and channel density, we perform linear regressions on the equilibrium channel density data provided in Fig. S7† and use these steady-state empirical expressions to identify the initial channel densities at 0 mV, N_{D0} , and voltage dependences, m , as given by:

$$N_D(V) = N_{D0}(mV^2 + 1) \quad (4)$$

Because the channels exhibit nearly instantaneous responses to changes in voltage (and thickness) (Fig. S7†), the time constant for electrocompressive thinning ($O \sim s$), τ_{ec} , dictates the speed by which changes in channel density occur as a result of voltage-induced reductions in thickness. This allows us to write an empirical first order differential equation of the form:

$$\frac{dN_D}{dt} = \frac{1}{\tau_{ec}}(N_{D0}(mV^2 + 1) - N_D) \quad (5)$$

to describe the dynamic changes in N_D . For DPhPC bilayers in hexadecane which do not undergo EC, eqn (4) is used to define channel density at all points in time. Similarly, values of α and τ_{ew} (Table 1) are used as before⁴³ to describe the dynamic fractional area growth *versus* voltage, given by:

$$\frac{dA_m}{dt} = \frac{1}{\tau_{ew}}(\alpha v^2 - A_m(t)). \quad (6)$$

Given that the total number of channels in the membrane is the product of nominal membrane area, $A = A_0(1 + A_m)$ and N_D , and the unit conductance of each channel is G_u , the nominal conductance is written as

$$C(V, t) = G_u \times N_D(V, t) \times A_0(1 + A_m(V, t)) \quad (7)$$

where A_0 is the area of the interface at zero bias.

Using eqn (4)–(7) and values in Table 1, we simulate dynamic changes in channel density and membrane area in response to a sinusoidal voltage and use these to compute the total current. Fig. 3A shows the changes in N_D and A_m *versus* time for a DPhPC AES formed in C16 subjected to a 10 mHz, 200 mV sinusoidal voltage. Without significant changes in thickness, the voltage induced changes in channel densities occur nearly instantaneously, which causes the dynamic response to remain in phase with the applied voltage. EW-driven changes in membrane area occur more slowly ($\tau_{ew} \sim 14$ s), resulting in a noticeable time lag behind the applied potential and causing a dc shift of $\sim +25\%$. At steady state, the amplitudes of normalized channel density and membrane area are 90% and $\sim 20\%$, respectively. But for AES that undergo significant thinning with increased voltage (*e.g.*, a DOPC AES in C10), changes in N_D are slower than those in A as seen in

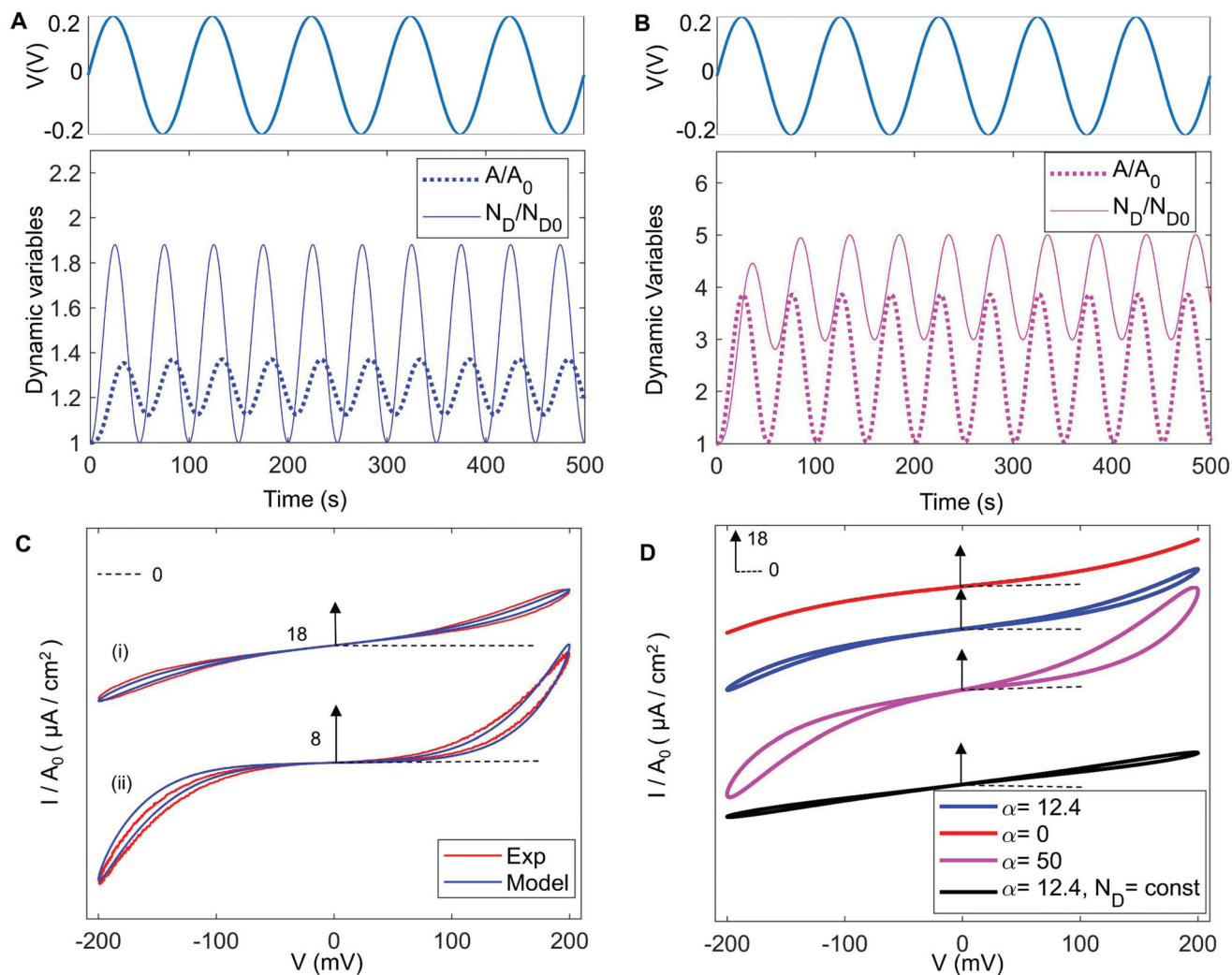


Fig. 3 Simulated dynamic responses of AES. Membrane area and channel density using EW and EC parameters for a DPhPC membrane in C16 (A) and DOPC in C10 (B), respectively, in response to 200 mV, 10 MHz sinusoidal voltage (top). Simulated I - V relationships for: (C) (i) DPhPC AES in C16, and (ii) DOPC AES in C10; and (D) DPhPC AES in C16 at various electro wetting conditions with dynamic channel density. The black trace in (D) predicts the response of the device at a constant channel density. Vertical scales denoted using arrow length and value. All currents are normalized per zero-volt initial area, A_0 . Applied bias consisted of a 200 mV bipolar sinusoidal voltage at 10 MHz, unless stated otherwise.

Fig. 3B. Note that this occurs because the rate of thinning limits the speed of gramicidin insertion in the membrane. Fig. 3C and Fig. S9† show the simulated nominal current *versus* voltage and time, respectively, at steady state for the same sinusoidal voltage input. Here, we see the models accurately capture the nonlinear changes in synaptic conductance that affect the induced current.

In Fig. 3D, we simulate the I - V response of a DPhPC AES in C16 at 10 mV for varying α values to investigate the sources of nonlinearity and hysteresis. By setting α to zero (*i.e.*, area is fixed), hysteresis vanishes and the nonlinear increase in current is explained by the instantaneous growth in channel density with voltage. Increasing α to a value of 50 amplifies both the total change in current and the hysteresis during a voltage. Further, keeping α at the measured value of 12.4 and setting N_D to be constant yields in a nearly linear relation-

ship with only a small amount of hysteresis. In contrast, the larger, slow increases in N_D for DOPC AES add additional I - V hysteresis and nonlinearity due to time-varying channel densities independent of the membrane area.

Short-term facilitation and depression in AES

Activity-dependent short-term plasticity (STP) enables synapses to adjust their conductance strength in ways that either facilitate (strengthen) or depress (weaken) the activity of the post-synaptic neuron. The I - V hysteresis demonstrated in Fig. 2 shows that at specific frequencies the AES exhibits a conductance that is dependent both on the present value and prior history of applied voltage. Because these hysteresis loops disappear at very low frequencies, the system can be classified as a volatile memristor for which the alterations in conductance return to an equilibrium level upon removal of the excitation.

The prior section demonstrates that for gramicidin-doped bilayers with symmetric lipid compositions these alterations occur due to reversible increases in both area and channel density, processes that occur at characteristic time scales governed by the dynamics of EW and EC, respectively.

Plasticity of synaptic elements is commonly assessed by recording the responses to multiple, successive voltage excitations.⁶⁵ Therefore, we stimulate our AES with a train of positive, rectangular voltage pulses and study the dynamic current responses. As compared in Fig. 4A, we consider gramicidin-doped AES membranes that have either symmetric and asymmetric lipid compositions—the latter, which we have previously shown can be used to enable asymmetric EW responses with respect to 0 mV.⁴² Specifically, we compare the behaviors of a symmetric DOPC bilayer in decane to an asymmetric membrane consisting of one DOPC leaflet and one leaflet con-

taining a 1 : 1 molar mixture of DOPC and 1,2-di-*O*-phytanoyl-*sn*-glycero-phosphocholine (DOPhPC)—a combination that exhibits an intrinsic dipole potential difference of -85 mV. Unlike a symmetric membrane that exhibits zero intrinsic potential, the net potential across an asymmetric membrane is the sum of the applied voltage and the intrinsic potential.⁴² This means that EW and EC are minimized when the applied potential is equal and opposite to the intrinsic potential, not at zero. Thus, the asymmetric membrane is larger in area and thinner at 0 mV than when $+85$ mV is applied. Here, we hypothesize that a voltage-dependent reduction in area and increase in thickness can be used to lessen the number of conductive channels in the membrane, thereby creating a depressive form of short-term plasticity.

Fig. 4B shows the raw ohmic current measured across a symmetric gramicidin doped DOPC membrane in response to

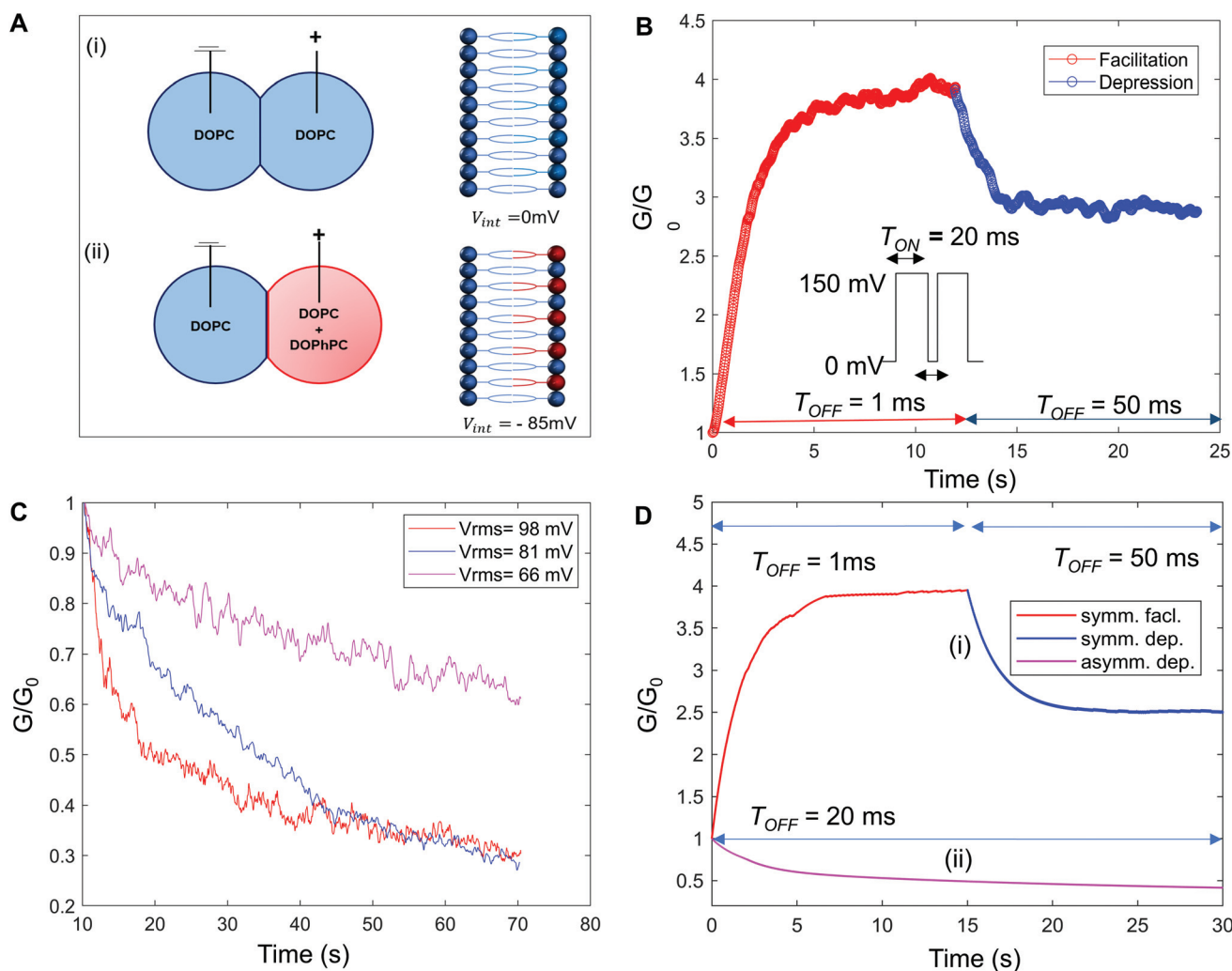


Fig. 4 Short-term plasticity in symmetric and asymmetric AES. (A) Cartoon depicting symmetric and asymmetric assembly of droplets and the interfacial membrane. (B) Accumulation and depression of current per unit area of the membrane for varying T_{OFF} values. (C) Depression of conductance of the device even with increased stimuli (voltage input) because of reverse EW stemming from dipole potential difference of asymmetric droplets. (D) Simulation of short-term facilitation and depression in symmetric (blue lines) and asymmetric AES (magenta line).

+150 mV, 50 ms ON pulses followed by 0 mV OFF periods. For the first 10 s when the OFF time is 1 ms (95.2% duty cycle, $V_{\text{RMS}} = 95$ mV), the peak current during ON times (normalized by the zero-voltage area) increases exponentially across many pulses with a time constant of 1.75 s. This type of facilitative short-term plasticity is consistent with the time for gramicidin channels/bilayer area to increase in response to a non-zero RMS voltage. With sufficient preceding rise in synaptic conductance, a change in the OFF time of the pulses to 50 ms (28.5% duty cycle, $V_{\text{RMS}} = 29$ mV) causes the membrane to gradually become less conductive as indicated by the reduction in ohmic current in Fig. 4B after 10 s. This depressing response occurs as the area of the membrane drops, the thickness increases, and the channel density lowers a smaller positive RMS voltage. However, the fact that the steady-state peak current for 50 ms OFF times is still higher than the initial value prior to pulse train excitation means that if only this stimulus were provided instead, a symmetric membrane will not exhibit depressive STP without sufficient facilitative STP first occurring.

Yet, depression in electrical synapses is more common,^{10,66} a trait that enables modulation of electrical coupling,⁶⁶ regulates response to the sensory surround and arousal states.¹⁰ Fig. 4C shows the peak ohmic current *versus* time for an asymmetric DOPC: DOPC + DOPhPC membrane containing gramicidin at three different positive V_{RMS} levels (varying duty cycle, equal amplitude). Representative I - V measurements for an asymmetric AES are provided in Fig. S10.† Here, unlike the response in Fig. 4B, we observe that current only decreases upon application of a positive voltage. This occurs because the net membrane potential drops when voltage increases from 0 mV to +100 mV. The amount of decrease varies with the RMS value, which is consistent with the idea that the membrane becomes less conductive (see Fig. S10†) when the area is small and the thickness is large which occurs at zero net potential. Quasi-static analysis (Fig. S11†) confirms that the interfacial area of an asymmetric AES responds to the transmembrane potential difference. However, we also observe the channel density to exhibit stronger increases with voltage at negative applied potentials, where the net membrane potential is larger, compared to positive stimuli. This effect is likely a combination of channel kinetics changing with the applied potential and the thickness of the membrane varying with respect to net membrane potential.

Fig. 4D(i) and (ii) show simulated peak currents for symmetric and asymmetric AES subjected to unipolar square pulse inputs (150 mV, 20 ms ON, 0 mV, variable duration T_{OFF}). These trends bear close resemblance to the measured behaviors of symmetric and asymmetric AES devices as seen in Fig. 4B and C. For the asymmetric system, the voltage dependent channel density equation (eqn (5)) and electrowetting equation (eqn (6)) are modified to accommodate a net bias input of $\nu = \nu_{\text{appl}} + \nu_{\text{int}}$.

AES enable variable synchronization of neurons

Electrical synapses synchronize the activities of many neurons^{67,68} by allowing fast, threshold-independent sharing

of action potentials and ionic gradients. The AES presented in this paper share several traits in common with ES, including a variable conductance that occurs at biologically relevant levels of voltage and which spans nominal conductance ranges similar to ES. Therefore, to demonstrate that our voltage-dependent AES can synchronize neurons, we employ our model of AES conductance and simulate in MATLAB the responses of two Hodgkin–Huxley (H–H) neurons⁶⁹ connected by our adaptive AES (illustrated in Fig. 5A). The variable resistances in the neurons represent the voltage-gated sodium and potassium channels in addition to leakage pathways. The neuron on the left is stimulated with a dc current density of $10 \mu\text{A cm}^{-2}$, a level which is sufficient to elicit repeated oscillations. This injection charges neuron 1, whereby at a sufficient voltage the sodium channels open in neuron 1, causing rapid depolarization of the cell. Then, at sufficiently positive voltage, potassium channels open, hyperpolarizing the cell and resetting the voltage. This nonlinear, oscillatory response creates an action potential with a spiking period of 15 ms. By connecting two neurons with a threshold-independent AES, some of the injected current can also enter neuron 2, where it can similarly charge and fire. The amount of current through the AES depends on its conductance, which in this application is modulated by the relative neuron voltages, V_1 and V_2 . For these simulations, we use the parameters defined in ESI Table 1† for a gramicidin doped DOPC membrane in C10. The voltage-dependent membrane capacitance of the AES ($C_m = 0.496 \mu\text{F cm}^{-2}$) is also included in the calculation, and we assume the active areas of the neuron and synapse (zero-volt area) are equal to the DIB area ($3.3 \times 10^{-4} \text{cm}^2$) observed in experiments.

Fig. 5B shows the simulated voltages of both neurons *versus* time; Fig. 5C and D show the computed nominal resistance of the AES and the spiking ratios (spike count of neuron 2 to that of neuron 1) and time lag between adjacent spikes, respectively. The simulation shows that only neuron 1 produces an action potential (Fig. 5B(i)). The initial AES resistance ($\sim 80 \text{M}\Omega$) limits charging of neuron 2, resulting in only sub-threshold oscillations with amplitudes of 6–8% of V_1 . This response shows that initially neuron 2 is completely desynchronized from action potentials from neuron 1.

However, over time the difference in neuron voltages (38 mV RMS) lowers the resistance of the AES to reduce to $\sim 34 \text{M}\Omega$ *via* bilayer area growth and increased channel density (Fig. S12†). Neuron 2 begins generating action potentials when the AES resistance falls below $74 \text{M}\Omega$. This voltage-dependent adaptation allows increasingly more current to enter neuron 2 and further increases the rate of action potential generation. Fig. 5B(ii–iv) show this adaptation; here we see neuron 2 exhibiting action potentials with increasing frequency over time (total simulation time is 100 s to capture the full adaptation of the AES). The spiking ratio increases incrementally during this time, where after approximately 67 s, when the AES resistance drops below $\sim 40 \text{M}\Omega$, every action potential by neuron 1 coincides with one from neuron 2. While synchronized in frequency at this point, action potentials from neuron 2 still lag

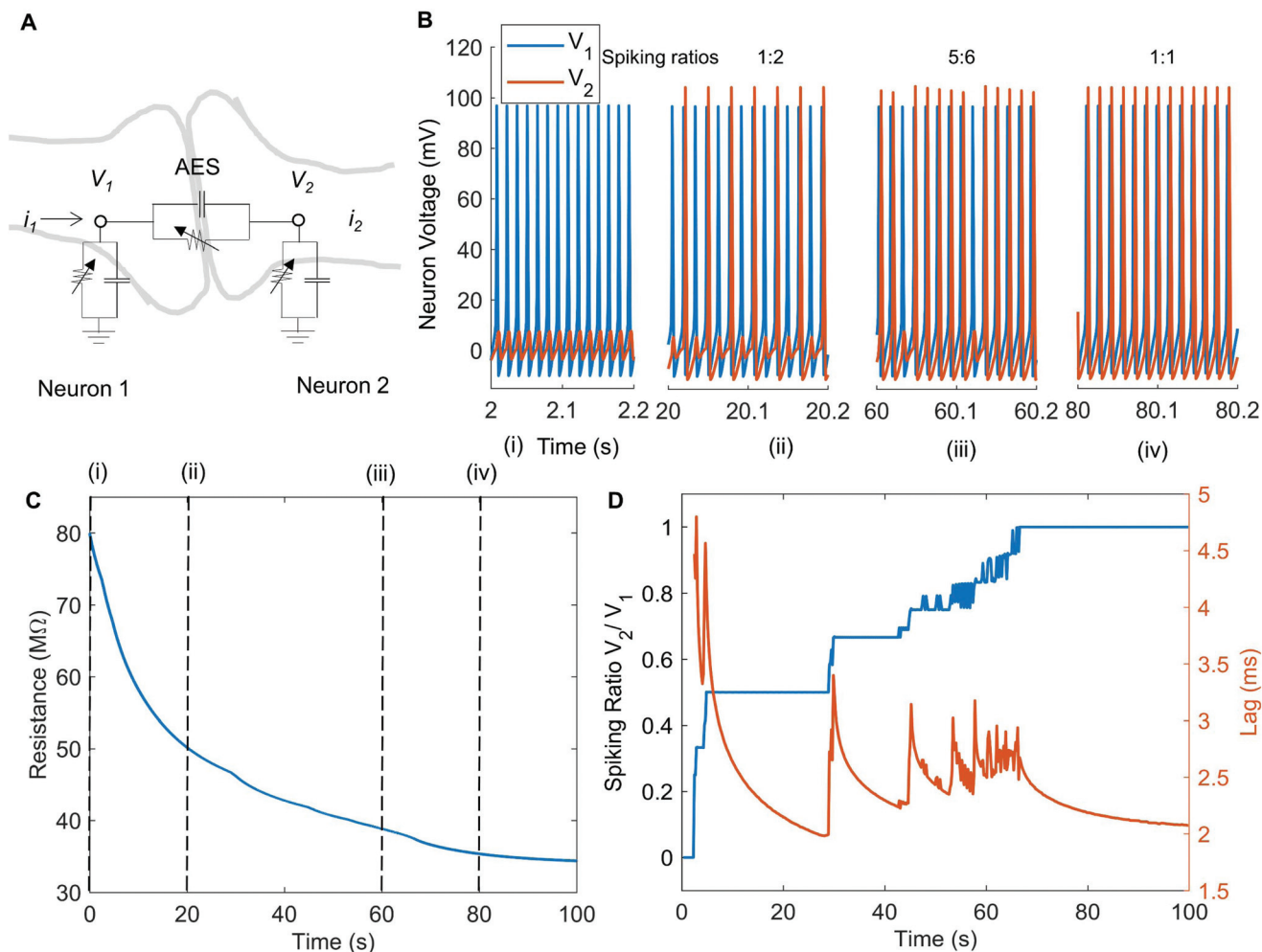


Fig. 5 H–H neuron synchronization through AES plasticity. (A) Illustration of two H–H neurons joined by an AES. (B) Simulated neuron voltages versus time in response to a constant injected current into Neuron 1. (C) AES resistance versus time during adaption. (D) Neuron voltage spiking ratios and lag time between neuron spikes versus time.

by ~ 2 ms those from neuron 1. This time lag decreases non-monotonically during the AES adaptation; specifically, it appears to decrease exponentially in time for each period of constant spiking ratios.

An electrical synapse mimic for synchronizing spiking neurons—*e.g.*, for use in artificial neural networks—has real advantages compared to devices mimicking the one-direction, threshold dependent variable conductance of a chemical synapse. The bidirectional conductance of the AES means that if neuron 2 were stimulated with current instead, neuron 1 could become synchronized. Additionally, the lack of a voltage-threshold for ion channel formation allows ions to quickly pass through the AES to charge and fire neuron 2 with minimal lag. In contrast, a memristive synaptic mimic constructed using alamethicin⁴³ exhibits much slower channel insertion kinetics, which would prevent successful synchronization of the two neurons.

The simulation shows how the voltage-dependent plasticity of an AES can be used to adaptively couple spiking neurons,

and the conditions for the calculations require some tuning to demonstrate this functionality. Specifically, initial channel density, N_{DO} , and the voltage dependency, m , of the synapse are set to 6.5×10^6 and 2×10^9 , respectively, to ensure that the device exhibited an initial resistance of 80 M Ω and a large reduction in resistance at RMS voltages below 50 mV. In contrast, smaller values of N_{DO} and m (such as those in Table 1) result in a highly resistive junction that does not sufficiently reduce to cause firing in neuron 2. Nonetheless, the parameters used closely match experimentally obtained values on a symmetric DOPC membrane in C10 by mechanically reducing the membrane area after bilayer formation (see ESI Table S1† for measured values and Fig. S5† for effect of membrane area on electrowetting sensitivity). In contrast, while an asymmetric AES displays short-term depression under a sufficiently large positive potential (see Fig. 4C in the manuscript), the same device is unable to desynchronize H–H neurons because the average voltage across a highly conductive AES (required to synchronize neurons) is insufficient for appreciably changing

AES. Fig. S13† summarizes the response of an initially conductive AES placed between two Hodgkin–Huxley neurons.

In our simulation, the ratio of neuron area to synapse area is a parameter that strongly impacts the amount of nominal current flowing through the AES. This is based on the fact that Hodgkin–Huxley equations are normalized per area of the neuron membrane. Therefore, when the active area of the neuron is larger than that of the synapse, the synapse is considerably less conductive than the neurons. This change means that even less current passes through the AES, lowering the rate of firing of neuron 2. Less current through the AES also causes the V_{RMS} difference between the neurons to shrink to 27 mV, which subsequently results in a smaller voltage-induced plasticity. Furthermore, higher neuron conductance means even larger reductions in AES resistance from the same initial value (80 M Ω) are needed to fully synchronize the two neurons. For example, increasing the area ratio to just 10 raises the final synapse resistance to 50 M Ω , a value that now only results in sub-threshold voltage oscillations in neuron 2. This demonstrates that effectively matching the impedances of the neurons and the adjoining synapse is important for making use of voltage-activity plasticity in hardware-based neural circuits.

Conclusion

We present a threshold-independent, artificial electrical synapse that exhibits volatile memristance and which mimics the composition, structure, and transport properties of an electrical synapse found in the mammalian brain. Our unique, two-terminal AES consists of a lipid bilayer membrane doped with gramicidin peptides that form conductive ion channels through the lipid bilayer. Like connexins in ES, these channels feature an end-to-end connection across both leaflets of the membrane and do not require a threshold-voltage to conduct ions. The current–voltage relationships of gramicidin-based AES exhibit pinched hysteresis at excitation frequencies between 10–100 mHz. Experiments reveal that the volatile memristive device is affected by two voltage-dependent state variables: the gramicidin channel concentration per unit area and membrane area, the product of which dictate the total number of channels in the AES and, thus the conductance of the device. In addition, the current–voltage relationships show that combinations of peptide concentration, oil composition, and lipid type and arrangement modulate the conductivity, nonlinearity, and hysteresis of the AES. Using a mathematical model of AES developed from empirical expressions for both state variables, we also show that the voltage-induced plasticity in an AES can dynamically synchronize the firing of two HH neurons, illustrating one of the key uses of ES in neural networks.

Like the brain, ES functionality in neural networks may also enable greater cognitive power in neuromorphic circuits. Our AES devices, unlike most neuromorphic devices, mimic the continuously-variable conduction, bidirectional ion transport,

and activity-dependent plasticity of ES. These results also highlight that a biomolecular approach is one that enables uniquely modular transport properties and tunable plasticity that can be achieved at biologically relevant voltages.

Experimental

Materials

The aqueous droplets in each DIB-based AES consist of phospholipid vesicles, salt, and buffering agent in 99.99% pure de-ionized water. Sodium chloride (NaCl), 3-(N-morpholino) propanesulfonic acid (MOPS), sodium hydroxide (NaOH), agarose (C₁₂H₁₈O₉), *n*-hexadecane (C₁₆, 99% pure), *n*-decane (C₁₀, 99% pure), ethanol, isopropyl alcohol was purchased from Sigma Aldrich. DPhPC, DOPC, and DOPhPC lipids are obtained from Avanti Polar Lipids, Inc. and used without further purification. Lipid vesicles are prepared and stored at a concentration 2 mg ml⁻¹ in aqueous buffer containing 500 mM NaCl, 10 mM MOPS at pH of 7.0 achieved *via* NaOH titration as described elsewhere.⁵⁵ Hydrogel (2% (w/v)) electrode coatings are prepared from agarose powder and the same buffer. A stock solution of gramicidin in ethanol (10 mg mL⁻¹) is diluted with the lipid vesicle solutions to yield the desired final concentration.

Methods for DIB formation

DIBs are formed between two, 300 nL aqueous droplets suspended agarose coated wire-type electrodes in an oil-filled reservoir as described elsewhere.⁷⁰ The oil reservoir and droplets are centered above a 4 \times objective lens on an Olympus IX50 inverted microscope. The positions of both electrodes are controlled by three-axis micromanipulators. A lipid bilayer forms spontaneously within a minute after bringing droplets into contact following a brief incubation period to ensure lipid monolayer assembly. Bottom-view images (Fig. 1B) of DIB-based AES obtained using a QIClick-F-M-12-C (SN: Q31274) camera controlled by MicroManager software are used to estimate membrane area for computing specific capacitance and thickness. Based on the work by Taylor *et al.*,⁵⁵ a correction factor of 1.773 is used to account for membrane ellipticity due to sagging droplets.

Electrical measurements

Current measurements are made using an Axopatch 200B patch clamp amplifier and Digidata 1440 data acquisition system (Molecular Devices). All recordings are made at room temperature with appropriate shielding using a well-grounded Faraday cage in place to minimize noise. Necessary input voltage waveforms are generated using Hewlett–Packard 3314A function generator and customized LabVIEW VI codes with NI four channel analogue output module (NI 9263). Outputs from these sources are input to the headstage of the Axopatch 200B through the external input to the amplifier. Confirmation of bilayer formation and measurements of nominal capacitance stems from the bilayer's current response to a 10 mV, 350 Hz triangular voltage waveform input as discussed earlier.⁵⁵

Sinusoidal cyclic voltammetry scans at various sweep rates are performed on the bilayer to generate the I - V relationships.⁷¹ The pinched hysteretic loops presented in Fig. 1 are obtained after filtering the residual capacitive current resulting from the lipid membrane as described elsewhere.⁷² The short-term plasticity behavior is studied using rectangular voltage pulses at varying duty cycles.

Simulating the model

We numerically simulate the hysteretic responses and short-term plasticity of our AES and the variable synchronization of Hodgkin-Huxley neurons using the described model and measured parameters (e.g. Table 1) in MATLAB.

Conflicts of interest

There are no conflicts to declare.

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